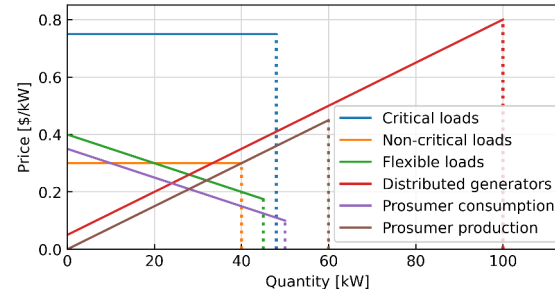


Background and Motivation

- **Grid-edge resources** can improve flexibility and **service restoration** in distribution systems.
- Direct load control poses **privacy** and **autonomy** concerns.
- **Transactive energy systems** can engage customers through price signals; their **use during outage conditions** is a topic of emerging research.

This **transactive energy system** engages a variety of **market participants** who value service restoration through **utility functions**.



The **primal-dual algorithm** is used to compute the **competitive equilibrium** and **maximize social welfare**.

Algorithm 1 Algorithm for transactive energy market

Input: Customer utility functions and resource limits

Output: Optimal market price, $\bar{\lambda}$

```

1: Initialize market price,  $\lambda_k = \lambda_0$ , done = False
2: while not done do
3:   Solve resource-level optimizations to maximize customer surpluses at price  $\lambda_k$ .
4:   Check for power flow, voltage violations.
5:   Calculate the updated price ( $\lambda_{k+1}$ ).
6:   if ( $|\lambda_{k+1} - \lambda_k|/\lambda_k \leq 0.00001$ ) then
7:      $\bar{\lambda} = \lambda_k$ , done = True
8:   else
9:     update market price,  $\lambda_k = \lambda_{k+1}$ 
10:  end if
11: end while
12: return  $\bar{\lambda}$ 

```

Optimization and modeling

A. Resource-level optimization

1. Critical and non-critical loads

If the market price is low enough, they consume their entire demand.

2. Flexible loads

Alter their consumption to maximize consumer surplus based on the market price and their utility functions.

3. Distributed generators

Alter their production to maximize producer surplus based on the market price and their utility functions.

4. Prosumers

Determine their optimal market consumption, generation consumed on-site, and generation sold to the market to maximize the sum of their consumer surplus and their producer surplus.

B. Power flow and voltage constraints

We adopt a **3-phase linear DistFlow** model and introduce slack variables to determine the **power flow and voltage violations**.

$$p_{i\varphi}^{s+}, p_{i\varphi}^{s-}, q_{i\varphi}^{s+}, q_{i\varphi}^{s-}, v_{i\varphi}^{s+}, v_{i\varphi}^{s-}$$

C. Price update equation

$$\lambda_{k+1} = \lambda_k + \gamma \sum_{i \in \mathcal{N}} \sum_{\varphi \in \Phi} (p_{i\varphi}^{s+} - p_{i\varphi}^{s-} + v_{i\varphi}^{s-} - v_{i\varphi}^{s+})$$

Increase if demand > supply

Decrease if demand > supply

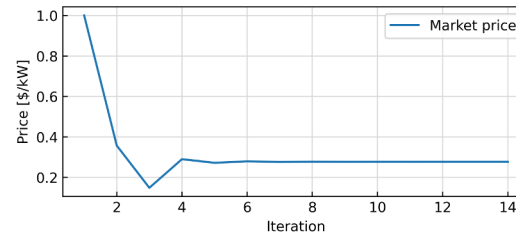
Increase if overvoltage, decrease if undervoltage

Numerical Results

The proposed approach is implemented on a **modified IEEE 123-bus** test system. It is modeled in **Pyomo** and solved using **GLPK**.

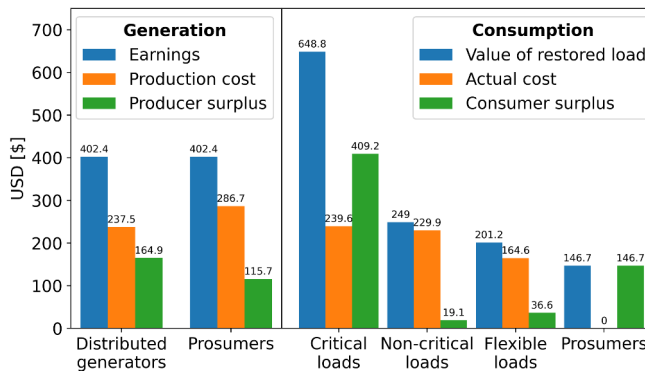
A. Market Price

The simulation converged to an optimal market price of 0.277 \$/kW in 12.7 seconds.

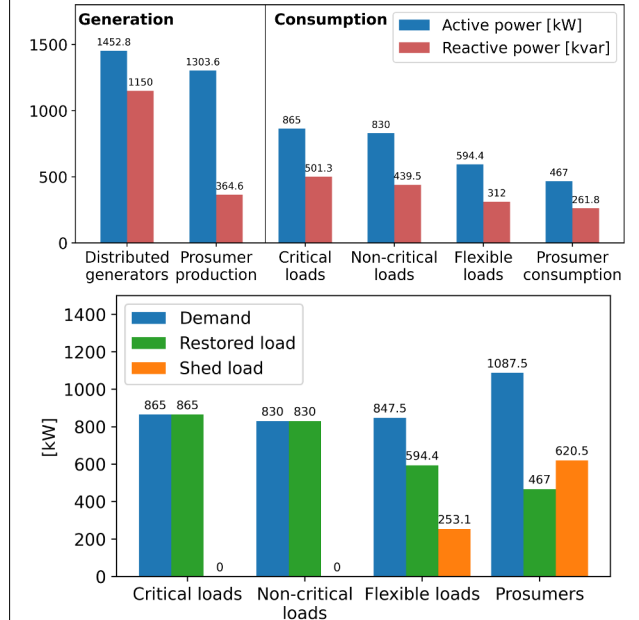


B. Customer Costs

Overall social welfare = sum of surpluses (\$892.2).



C. Service Restoration



Conclusions

- Market mechanism for grid-edge flexibility and DERs to **aid in service restoration**.
- System **resilience** is improved through decreased shed load.
- Utility functions must represent **the accurate value of lost load** during an outage for this approach to be **equitable**.