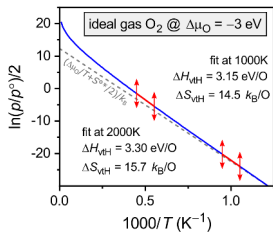


Chemical potential analysis vs van't Hoff



Solid state enthalpy and entropy (δH^r , δS^r)

$$\Delta G^{\text{tot}} = [\Delta G(M_{\text{q}}\text{O}_{1-\delta}) - \Delta G(M_{\text{q}}\text{O})] + \delta \Delta \mu_{\text{O}}$$

$$= [\Delta H^r - T \Delta S^r] + \delta \Delta \mu_{\text{O}}$$

$$\frac{\partial}{\partial \delta} \Delta G^{\text{tot}} \approx \delta G^{\text{tot}} = 0 \Rightarrow \delta H^r - T \delta S^r + \Delta \mu_{\text{O}} = 0$$

Shortcomings of van't Hoff $\frac{1}{2} \ln \frac{p}{p^0} = \frac{1}{T} \frac{\Delta H_{\text{vH}}}{k_B} + \frac{\Delta S_{\text{vH}}}{k_B}$

- Convolution of solid state and gas phase properties
- Non-linearity due to gas phase term
- No analysis of T -dependence, $\delta H^r(T)$ and $\delta S^r(T)$

Chemical potential method

$$-\Delta \mu_{\text{O}}(T)|_{\delta} = \delta H^r(T, \delta) - T \delta S^r(T, \delta)$$

$$\approx \delta G^r(T, \delta) = g_0 + g_1 T + g_2 T^2 + \dots$$

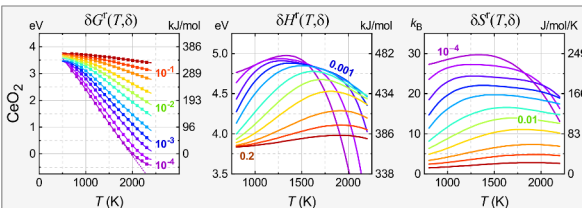
polynomial expansion in T

$$\delta S^r(T) = -\frac{d}{dT} \delta G^r(T)$$

$$\delta H^r(T) = \delta G^r(T) + T \delta S^r(T)$$

decomposition of δG^r into δH^r and δS^r

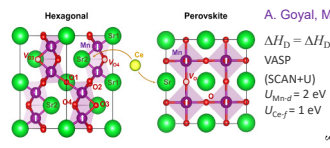
Chemical potential analysis of simulated (p_{O_2}, T) data (validated CeO₂ defect model)



- Strong T -dependence of δH^r and δS^r
- Physical origin: Defect ionization
- Large electronic entropy due to charged V_{O}^{2+}

SL, JACS 146, 14114 (2024)

Equilibria with interacting (neutral) defects



A. Goyal, M.D. Sanders, R.P. O'Hayre, SL, PRX Energy 3, 013008 (2024)

$\Delta H_{\text{O}} = \Delta H_{\text{D}}^{\text{ref}} + \Delta \mu_{\text{O}}$
VASP
(SCAN+U)
 $U_{\text{Mn}} = 2 \text{ eV}$
 $U_{\text{Ce}} = 1 \text{ eV}$

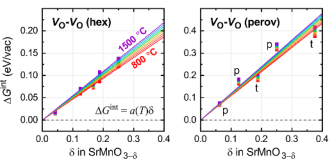
Free energy of defect interaction

Non-interacting: $\square_{\text{V}_\text{O}}$
Interacting defects: $\square_{\text{V}_\text{O}} \square_{\text{V}_\text{O}}$, $\square_{\text{V}_\text{O}} \square_{\text{V}_\text{V}}$, $\square_{\text{V}_\text{O}} \square_{\text{V}_\text{Ce}}$

$$\Delta E_i^{\text{int}} = \Delta H_{\text{D},i}(nV_{\text{O}}) - n \times \Delta H_{\text{D}}(V_{\text{O}})$$

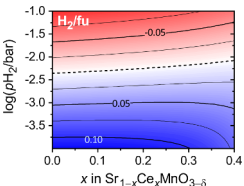
$$\Delta G_i^{\text{int}} = -\frac{k_B T}{n} \ln \int (g_i \exp(-\Delta E_i^{\text{int}}/k_B T))$$

$$\Delta G_i^{\text{int}}(T) = (a_0 + a_1 T) \delta \quad \text{parameterization}$$



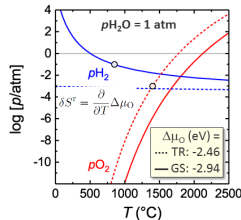
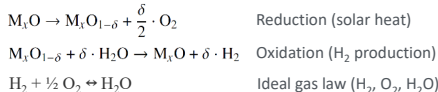
$$\Delta G_i^{\text{tot}} = f_i (x_V (\Delta H_{\text{D}} + \Delta G_{\text{D}}^{\text{int}}) + k_B T (x_V \ln(x_V) + (1-x_V) \ln(1-x_V)))$$

- Non-interacting: $3\delta = \frac{\exp(-\Delta H_{\text{D}}/k_B T)}{1 + \exp(-\Delta H_{\text{D}}/k_B T)}$ too large at high conc
- Interacting: slightly too low
- Adjusted ΔH_{D} (by $\sim 0.2 \text{ eV}$): essentially perfect
- T -dependence correct
- Phase transition from ΔG^{tot}



- SCM splits water, but only at low H₂:H₂O
- little benefit of Ce
- Enthalpy/entropy tradeoff

Impact of defect mechanism on STCH performance

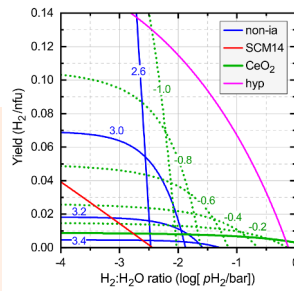


Capacity – yield tradeoff

- higher $\delta_{\text{ed}} \Rightarrow$ lower p_{H_2}
- defect interactions bad
- charged defects good

Hypothetical systems

- limited gains via ΔH_{r} in CeO₂
- high capacity and yield via defect ionization energies

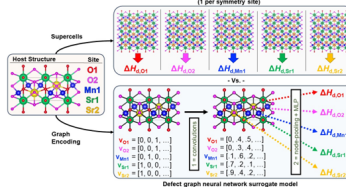


SL, J Chem Phys, 148, 071101 (2018)

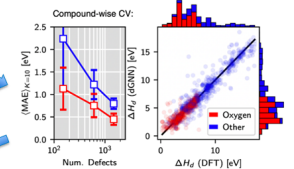
SL, JACS 146, 14114 (2024)

Defect Graph Neural Network

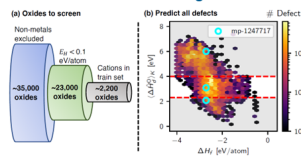
Model: HT-DFT + dGNN. Suppress vacancy defect DFT relaxations (1 per symmetry site)



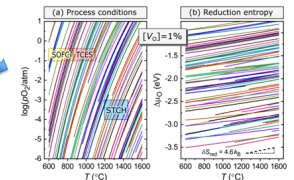
cross-validation



database screening



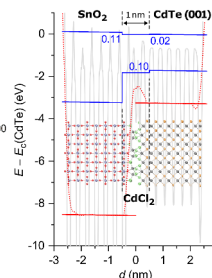
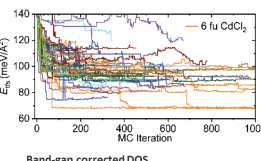
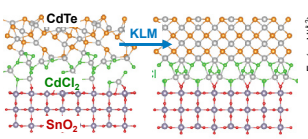
HT-thermodynamics



M.D. Witman, A. Goyal, T. Ogitsu, A.H. McDaniel, SL, Nature Comp Sci 3, 675 (2023).

Interface structure prediction

Sharan et al., Appl Phys Rev. 9, 041411 (2022)



- Interface structure prediction from first principles
- DFT relaxation: SCAN meta-GGA
- Electronic structure: Single-shot hybrid with onsite-potential (SSH+V)
- Statistical structure sampling (no assumptions)
- Incommensurate heterostructural interface
- Discovery of atomic CdCl₂ interlayer phase
- Near-perfect electronic structure and band offsets

E_g (eV)	SCAN	GW	SSH+V
SnO ₂	1.69	3.33	3.32
CdTe	0.99	1.69	1.71