

# Preventive Power Outage Estimation Based on A Novel Scenario Clustering Strategy

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## Contributions

- An optimal three-phase distribution system restoration model is established considering mobile energy resources (MERs) and the repair crews (RCs).
- A novel scenario clustering algorithm is proposed to reduce the scenario scale based on the accumulated nodal unserved load.
- The integration of MERs and RCs has been proved to significantly reduce the unserved load, and the representative scenarios can effectively preserve information of original scenarios.

## Three-phase Distribution System Restoration Model

### Objective function

$$\min. \sum_{t \in \Omega_T} \Delta t \sum_{i \in \Omega_B} \sum_{\phi \in \Omega_\phi} P_{i,\phi,t}^{peens}$$

### Power flow constraints

$$P_{i,\phi,t}^{MT} + P_{i,\phi,t}^{PV} + P_{i,\phi,t}^{MER} - P_{i,\phi,t}^D + P_{i,\phi,t}^{eens} = \sum_{k \in \theta(i)} P_{k,\phi,t} - \sum_{j \in \pi(i)} P_{j,\phi,t}$$

$$V_{i,\phi,t} = v_{i,\phi,t} - \Delta v_{i,\phi,t} - 2(\bar{r}_{ij,\phi} P_{ij,t} + \bar{x}_{ij,\phi} Q_{ij,t})$$

### Mobile energy resource allocation

$$\sum_{i \in N_m} y_{m,i,t} \leq 1, \forall m \in \Omega_M$$

$$\sum_{m \in \Omega_M} y_{m,i,t} \leq Cap_i, \forall i \in \Omega_{m \in \Omega_M} N_m$$

$$Z_{m,t} = 1 - \sum_{i \in N_m} y_{m,i,t}, \forall m \in \Omega_M$$

$$y_{m,i,t+\tau} + y_{m,i,t} \leq 1, \forall m \in \Omega_M, \forall i, j \in N_m,$$

$$\forall \tau \leq t_{m,i,j}^{\tau}, \forall \tau \leq \lfloor \Omega_T \rfloor$$

### Repair crew scheduling

$$Y_{ij,t} \leq \frac{\sum_{i=1}^t y_{m,i,t}}{v_{ij}}, \forall m \in \Omega_{RC}, \forall ij \in \Omega_P$$

$$Y_{ij,t} \leq Y_{ij,t+1}, \forall ij \in \Omega_P$$

## K-means-based Scenario Clustering

### Algorithm 1: Scenario Clustering

**1. Scenario generation:** Enumerate all possible faulted line scenarios based on the OPM outputs.

**2. Initialization:** For each  $s \in \Omega_S$ , compute:

$$E^s \in \operatorname{argmin} \sum_{t \in \Omega_T} \Delta t \sum_{i \in \Omega_B} \sum_{\phi \in \Omega_\phi} P_{i,\phi,t}^{peens}$$

**3. K-means clustering:**

**3.1.** Select a proper  $k$ .

**3.2.** Run the  $k$ -means algorithm by using the “sklearn” package. The algorithm aims to minimize the within-cluster sum of squares (WCSS):

$$WCSS \in \operatorname{argmin} \sum_{i=1}^k \sum_{s \in \Omega_{S_i}} \|E^s - \mu_i\|^2$$

where  $\mu_i$  is the centroid of cluster  $i$ .

**3.3.** Update the probability of clusters.

$$p(i) = \sum_{s \in \Omega_{S_i}} p(s)$$

## Numerical Simulations

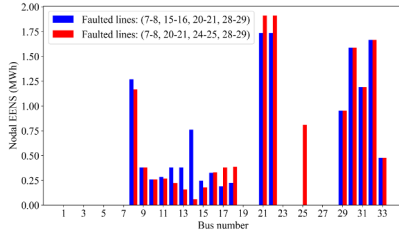


Fig. 1. Example of two nodal unserved load profiles.

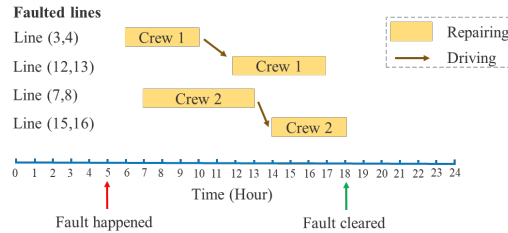


Fig. 3. RC schedule.

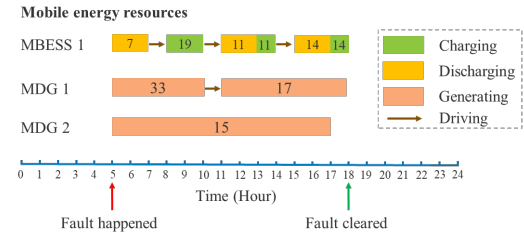


Fig. 4. MER allocation.

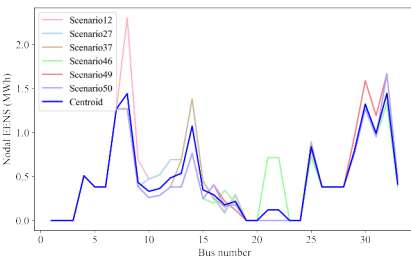


Fig. 2. Original scenarios and the centroid of Cluster 8.

Table 1 Comparison of the original and clustered scenarios without MERs.

Total EENS (MWh)	Unserved load ratio (%)	Original probability (%)	Clustered probability (%)
0 - 5	0 - 4.77	1.59	0
5 - 10	4.77 - 9.55	20.63	28.57
10 - 15	9.55 - 14.32	27.78	23.82
15 - 20	14.32 - 19.09	36.51	37.30
20 - 25	19.09 - 23.87	11.90	10.32
25 - 30	23.87 - 28.64	1.59	0

Table 2 Comparison of the original and clustered scenarios with MERs.

Total EENS (MWh)	Unserved load ratio (%)	Original probability (%)	Clustered probability (%)
0 - 5	0 - 4.77	37.30	37.30
5 - 10	4.77 - 9.55	23.81	26.98
10 - 15	9.55 - 14.32	36.51	34.92
15 - 20	14.32 - 19.09	2.38	0.79
20 - 25	19.09 - 23.87	0	0
25 - 30	23.87 - 28.64	0	0

## Conclusions

- The numerical simulation verifies that the representative scenarios can maintain the characteristics of the original scenarios.
- The improvement of the MER integration in the restoration process is also quantitatively evaluated.